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# Trajectory Pattern Mining on Road Networks



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## • Why

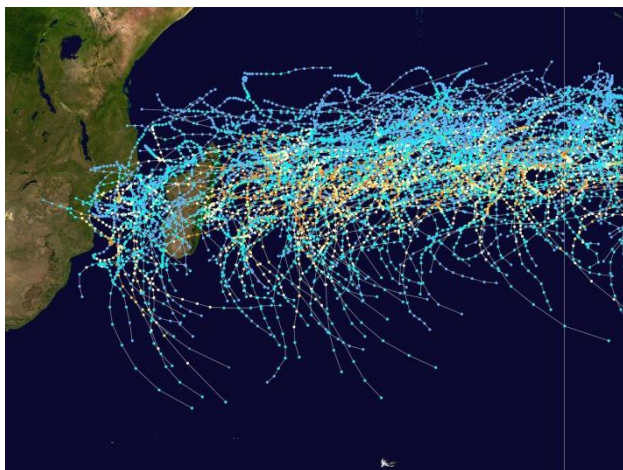
讲这个topic的目的，主要是因为之前讲过的关于轨迹的主题，很少考虑到路网的约束信息。而现实是，我们能得到的轨迹数据集更多情况下都是在路网中的，那么如何在有约束的情况下对具体任务进行模型的建立？所以这次topic就瞄准了路网中的轨迹模式挖掘。

## • Problems

如果已经考虑到路网存在的约束，我们又该考虑对轨迹添加哪些信息？或者说对于不同的任务，我们考虑的约束信息是否应该不同？等等这些问题都值得讨论和研究。

**Plus:**在这次准备的过程中，关键是如何讲想表达的主题和要讲到的论文算法结合到一起。经过思考后觉得选择两个相对较为简单的算法，既能将主题表达得比较清楚又能有相对的扩展。

- ✧ **Road Networks & Free Space**
- ✧ **Model Constraint Trajectories**
- ✧ **Problems & Algorithms**



hurricane

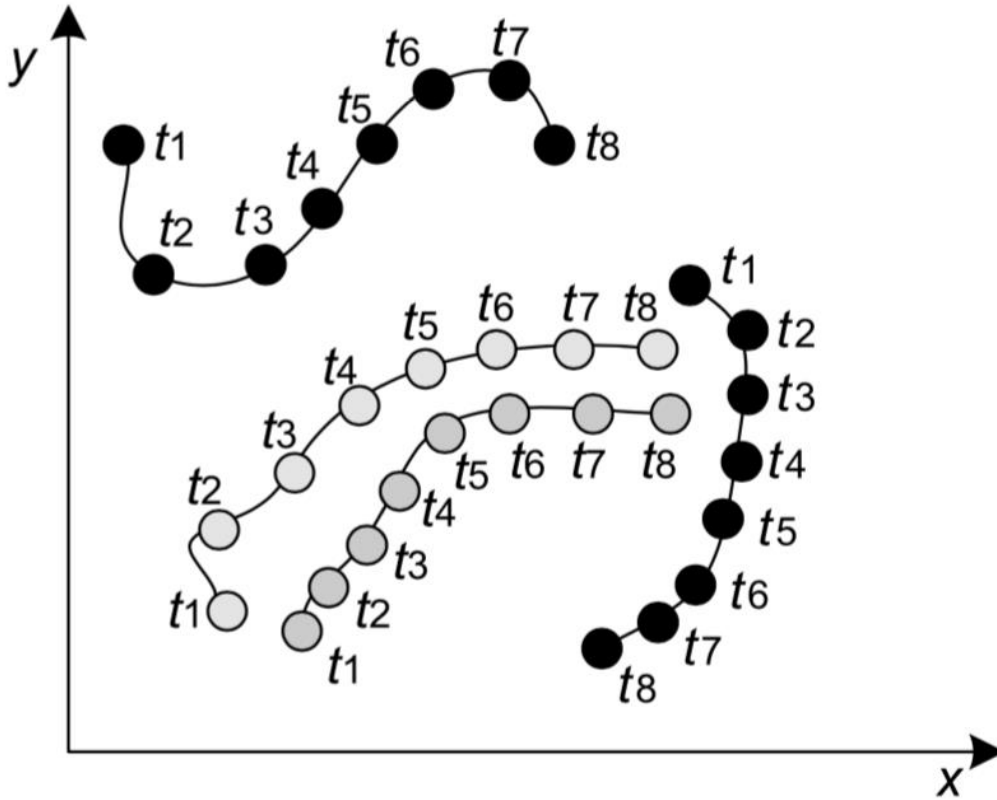
**V.S.**



Vehicle density

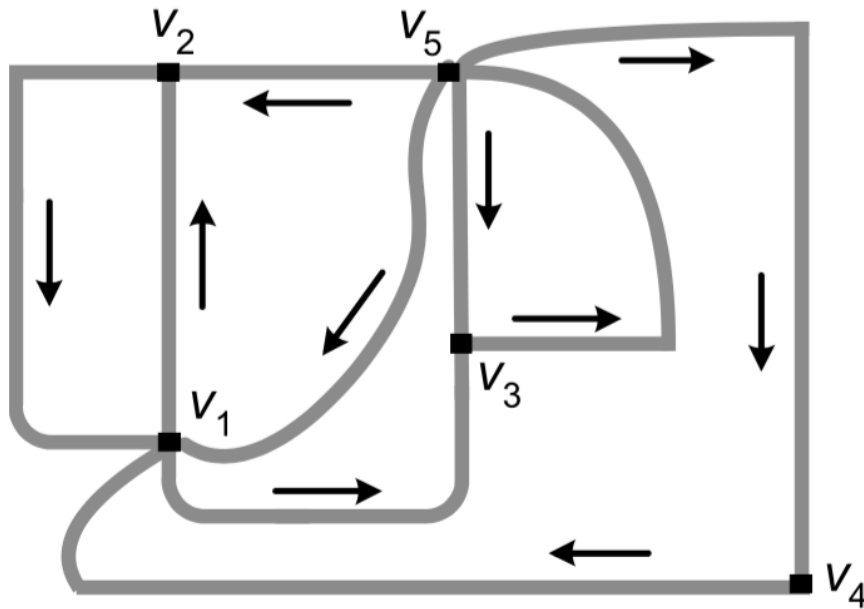


Animal migration



- ✧ **Objects move freely in any direction**
- ✧ **No underlying structure**
- ✧ **Euclidean distance based**

Example of four trajectories in the 2D Euclidean space

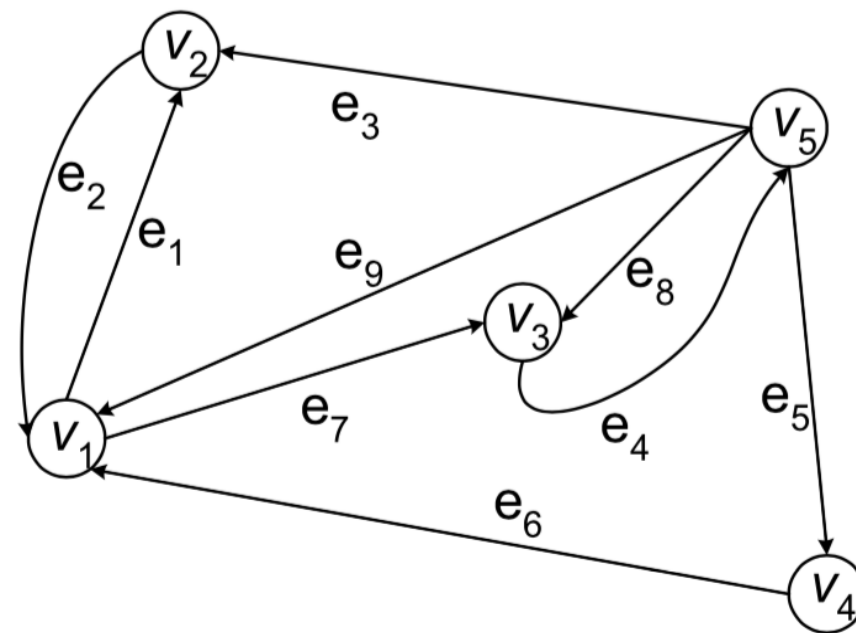
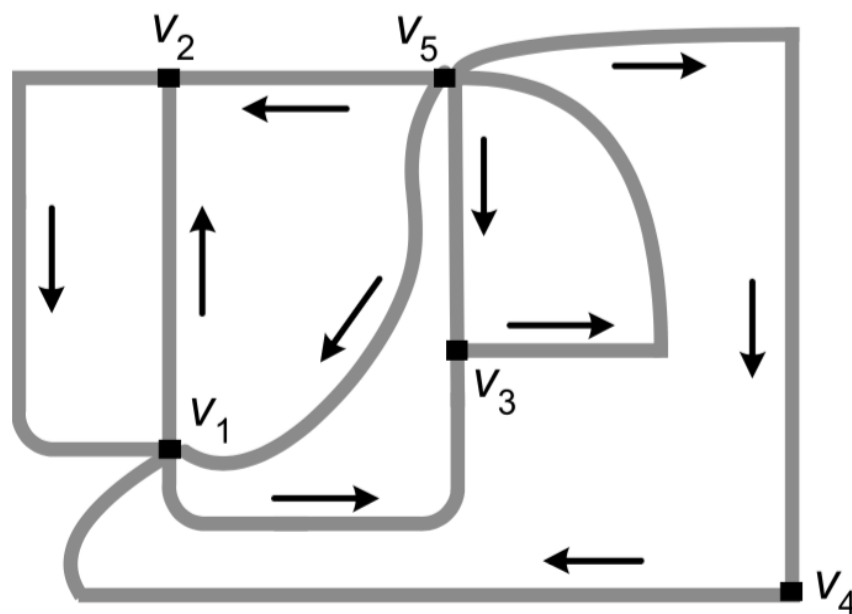


A road network

**Some constraints are:**

- ✧ **Directions**
- ✧ **Connectivity**
- ✧ **Speed**
- ✧ **Traffic flow**

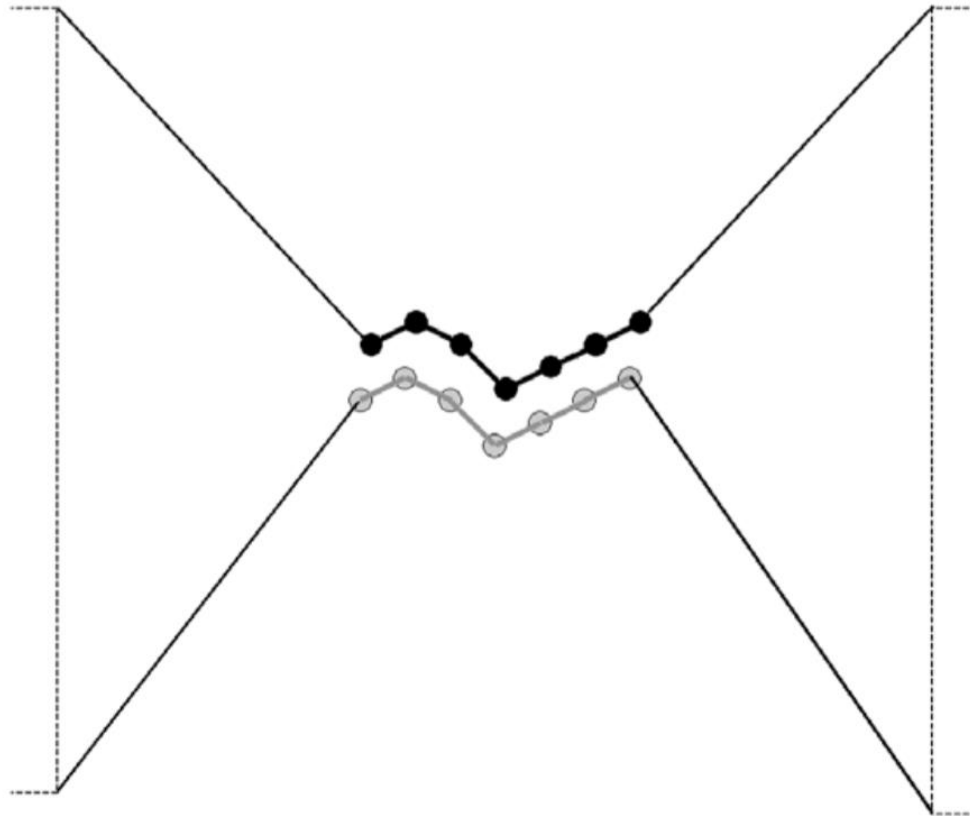
# An Natural Transformation → Directed Graph



For every edge, attributes include distance, time interval and other constraints.

## Similarity Measure

We can't calculate  $d(T_a, T_b)$  according to Euclidean distance.





$$d(v_i, v_j) = \begin{cases} 0, & \text{if } v_i = v_j, \\ \frac{c(v_i, v_j) + c(v_j, v_i)}{2D_G}, & \text{otherwise,} \end{cases}$$

$$D_G = \max\{c(v_i, v_j), \forall v_i, v_j \in V(G)\}$$

In a general way,  $c(v_i, v_j)$  is defined by Euclidean distance.

$$D_{net}(T_a, T_b) = \frac{1}{m} \sum_{i=1}^m (d(v_{ai}, v_{bi})) = \frac{1}{m} \sum_{i=1}^m (d(v_{bi}, v_{ai})) = D_{net}(T_b, T_a)$$

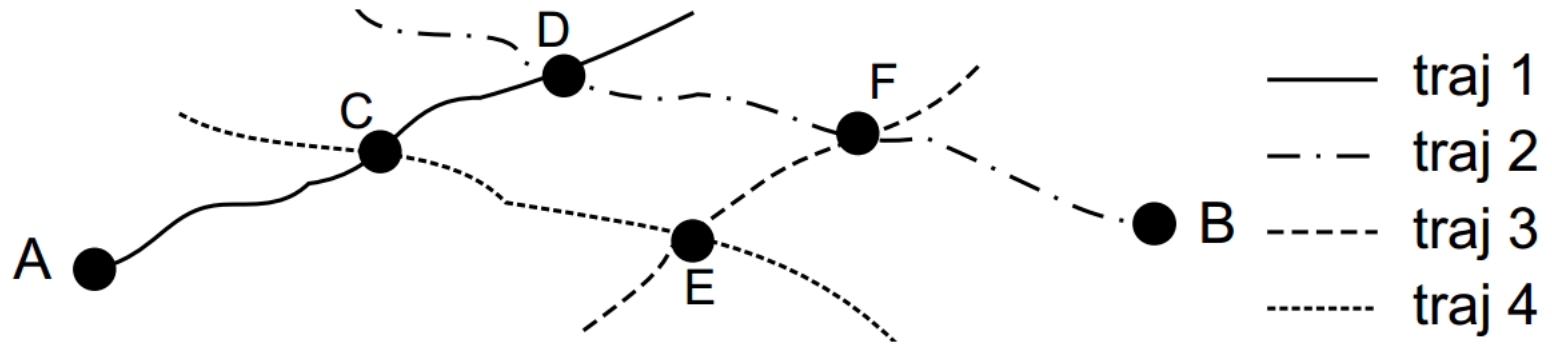
## Incorporating Time Information

$$D_{time}(T_a, T_b) = \frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|(T_a[i+1].t - T_a[i].t) - (T_b[i+1].t - T_b[i].t)|}{\max\{(T_a[i+1].t - T_a[i].t), (T_b[i+1].t - T_b[i].t)\}}$$

Finally

$$D_{total}(T_a, T_b) = W_{net} \cdot D_{net}(T_a, T_b) + W_{time} \cdot D_{time}(T_a, T_b)$$

## Popular Routes Mining



Objective:  $A \rightarrow B$      If  $A \rightarrow C \rightarrow D$  is a drive pattern, destination B would be ignored.

$$Pr(n_i \rightarrow n_j) = \frac{\text{number of trajectories on } (n_i, n_j)}{\text{number of trajectories on all outgoing edges}}$$

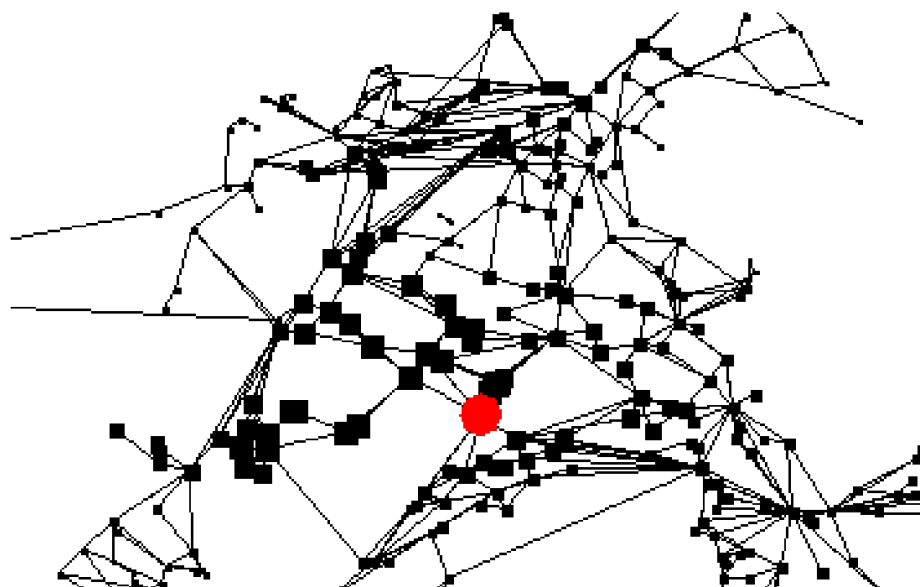
$$Pr_d(n_i \rightarrow n_j) = \frac{\sum_{traj \in (n_i, n_j)} func(traj, d)}{\sum_{traj \in \text{all outgoing edges}} func(traj, d)}$$

$$func(traj, d) = \exp(-dist_s(traj, d))$$

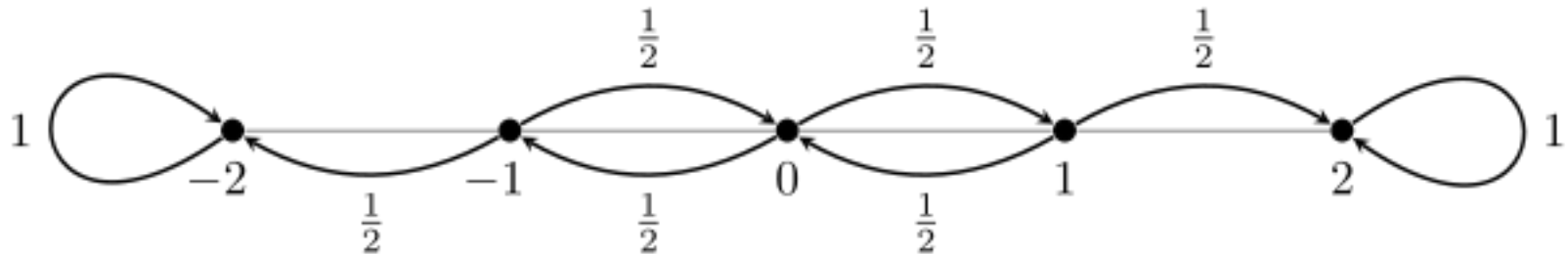
we can consider a travel on such a transfer network based on the turning probability as a **Random Walk** on a directed graph with the transition probability.

$$Pr^t(n_i \rightarrow d) = \sum_{j=1}^t p_{n_i, d}^j$$

This formula indicates how popular a transfer node  $n_i$  is, w.r.t. the given destination  $d$ .



In the mathematical theory of probability, an **absorbing Markov chain** is a Markov chain in which **every state** can reach an **absorbing state**. An absorbing state is a state that, once entered, cannot be left.



In a road network, destination can be regarded as an absorbing state and each intermediate node is a transient state.

## Absorbing Markov Chain

$$P = \begin{array}{c|cccc}
 & n_1 & n_2 & \cdots & n_m \\
 \hline
 n_1 & P(1, 1) & P(1, 2) & \cdots & P(1, m) \\
 n_2 & P(2, 1) & P(2, 2) & \cdots & P(2, m) \\
 \vdots & \vdots & \vdots & \ddots & \vdots \\
 n_m & P(m, 1) & P(m, 2) & \cdots & P(m, m)
 \end{array}$$

$$P(i, j) = \begin{cases} 1 & \text{if } n_i \text{ is an absorbing state \& } i = j \\ P_{rd}(n_i \rightarrow n_j) & \text{if } n_i \text{ is a transient state \& } i \neq j \\ 0 & \text{otherwise} \end{cases}$$

$$p_{n_i, d}^t = \sum_{n_k \in \text{TR}} (P^{t-1}(i, k) \cdot P(k, d))$$

$$Pr^t(n_i \rightarrow d) = \sum_{j=1}^t p_{n_i, d}^j$$

Probability from arbitrary node to destination.



$$\begin{aligned} Pr^t(n_i \rightarrow d) &= \sum_{j=1}^t p_{n_i, d}^j \\ &= \sum_{j=1}^t \sum_{n_k \in \text{TR}} (P^{j-1}(i, k) \cdot P(k, d)) \end{aligned}$$



$$n_i.\text{popularity}(d) = Pr^t(n_i \rightarrow d)$$

$$\rho(R) = \prod_{j=1}^i n_j.\text{popularity}(d)$$

Maximizing this formula ,we can get one popular route.

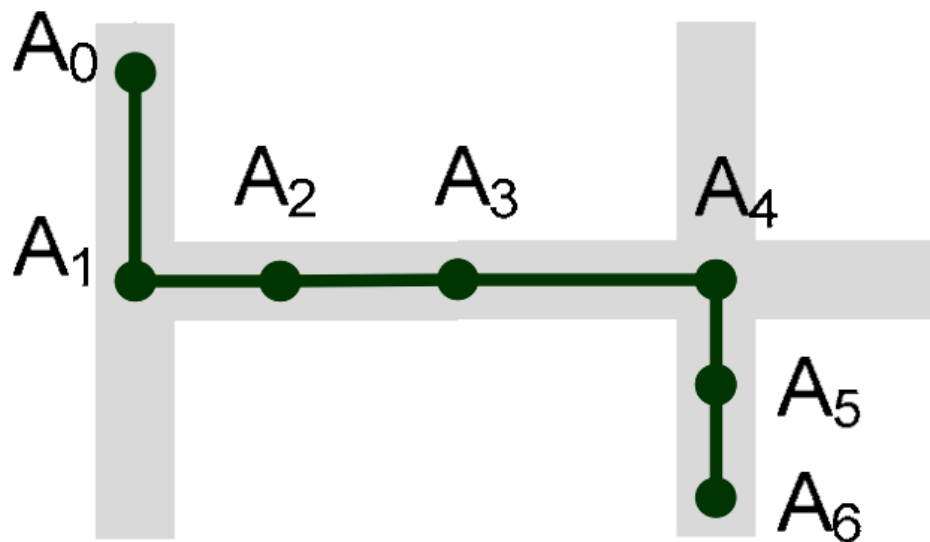


# Road Network Aware Trajectory Clustering

In the context of a road network, those objects have similar movement behavior with respect to the road segment.

**Atomic object:** Road segment

**Network proximity + Traffic flow + Speed limit  
+ ...**



$$TR = \{trid, l_0 l_1 \dots l_n\}$$

$$tf = \{trid, sid, l_k l_{k+m}\}$$

A trajectory has three t-fragments.

Base clusters:  $S = \{tf_i | TR(tf_i) \in \mathcal{T}, tf_i.sid = e.sid\}$

Dense-core:  $S = \arg \max_{S_i \in B} |S_i|$

Netflow:  $f(S_i, S_j) = |PTr(S_i) \cap PTr(S_j)|$

F-neighbor:  $N_f(S_i, n_u) = \{S_j | e^{S_j} \in L_{n_u}(e^{S_i}) \& f(S_i, S_j) > 0\}$

maxFlow-neighbor:

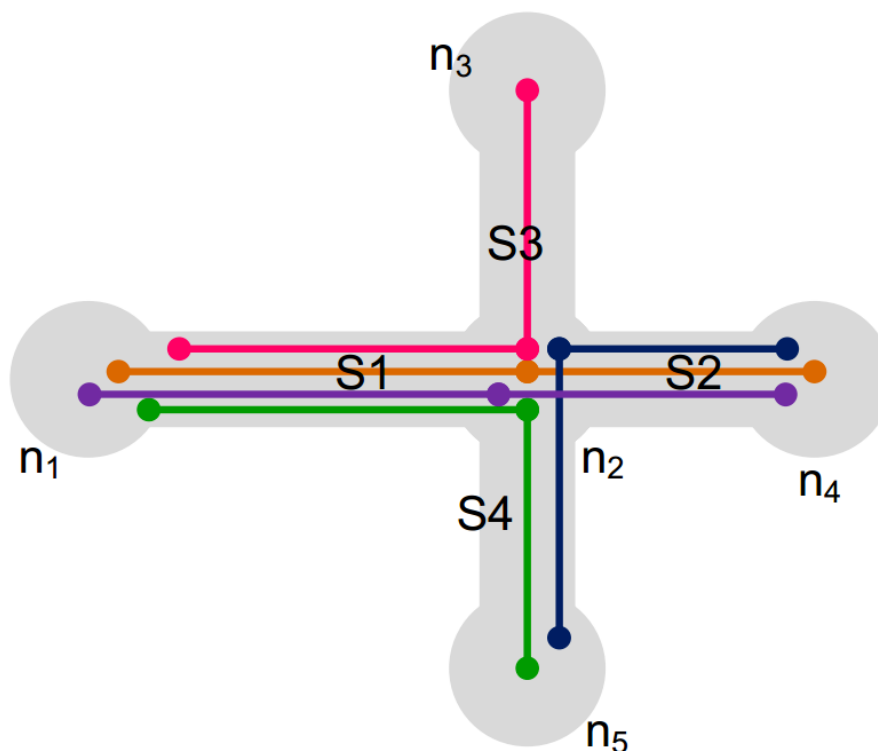


Flow cluster:

$$F =$$

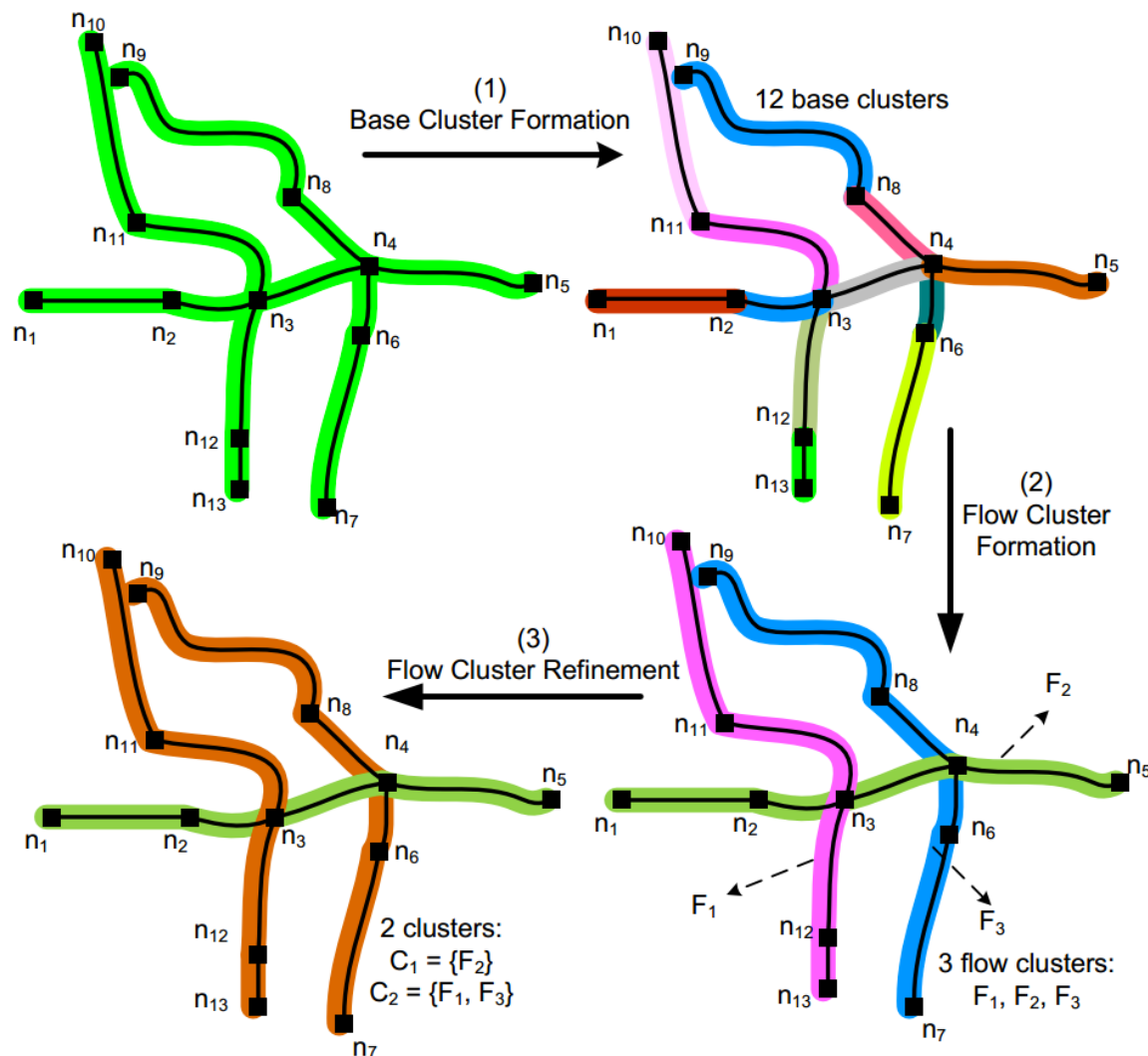
$$\{S_0, S_1, \dots, S_N\}, \text{ where } S_{i+1} \in N_f(S_i) (0 \leq i < N)$$

$$f(S_1, S_2) = 2, f(S_1, S_3) = 1 \dots$$



An example of base clusters and flow cluster

# Three phases of this algorithm





## 1. Base Cluster Formation

-- Skip

## 2. Flow Cluster Formation:

Density-based Flow Cluster Initialization: Dense-core of the set of base clusters.

Merging criteria: Flow + Density + Speed Limit



Flow factor:  $q = \frac{f(S, S_j)}{|PT_r(S)|}$

Density factor:  $k = \frac{d(S_j)}{d(S) + \sum_{S_i \in N_f(S, n_u)} d(S_i)}$

Speed limit factor:  $v = \frac{speed(S_j)}{\sum_{S_i \in N_f(S, n_u)} speed(S_i)}$

$$SF = w_q \times q + w_k \times k + w_v \times v$$

How to set ?

Which flow cluster should a base cluster belong to?

$$f_{n2n} / f_{c2n} > \beta ?$$



### 3. Flow Cluster Refinement

Hausdorff distance + DBScan

- 1.Chen Z, Shen H T, Zhou X. Discovering popular routes from trajectories[C] //Data Engineering (ICDE), 2011 IEEE 27th International Conference on. IEEE, 2011: 900-911
- 2.Lee J G, Han J, Li X, et al. Mining discriminative patterns for classifying trajectories on road networks[J]. IEEE Transactions on Knowledge and Data Engineering, 2011, 23(5): 713-726.
- 3.Lee J G, Han J, Li X, et al. Mining discriminative patterns for classifying trajectories on road networks[J]. IEEE Transactions on Knowledge and Data Engineering, 2011, 23(5): 713-726.
- 4.Han B, Liu L, Omiecinski E. Neat: Road network aware trajectory clustering[C] //Distributed Computing Systems (ICDCS), 2012 IEEE 32nd International Conference on. IEEE, 2012: 142-151.



5. Wu H, ZHENG B. Probabilistic Robust Route Recovery with Spatio-Temporal Dynamics[J]. 2016.

6. Li X, Han J, Lee J G, et al. Traffic density-based discovery of hot routes in road networks[C] // International Symposium on Spatial and Temporal Databases. Springer Berlin Heidelberg, 2007: 441-459.

# Thanks

